

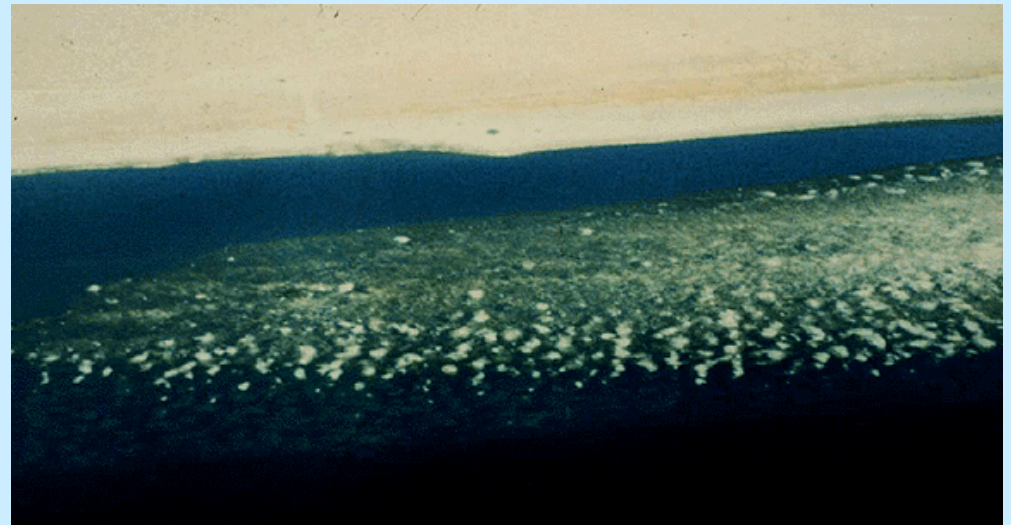
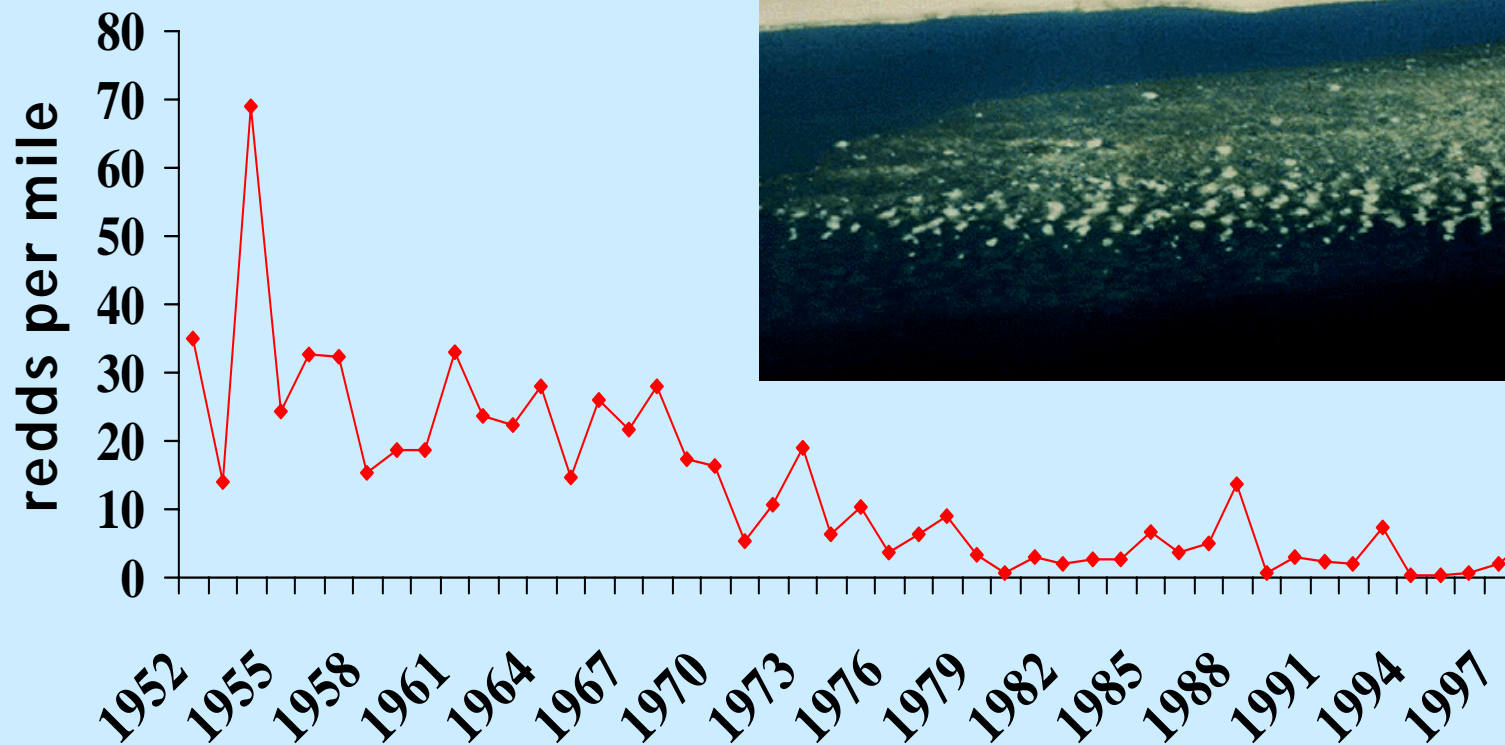
# Parsimonious stochastic models for quasi-extinction dynamics for stochastic vertebrate population processes

Elizabeth E. Holmes

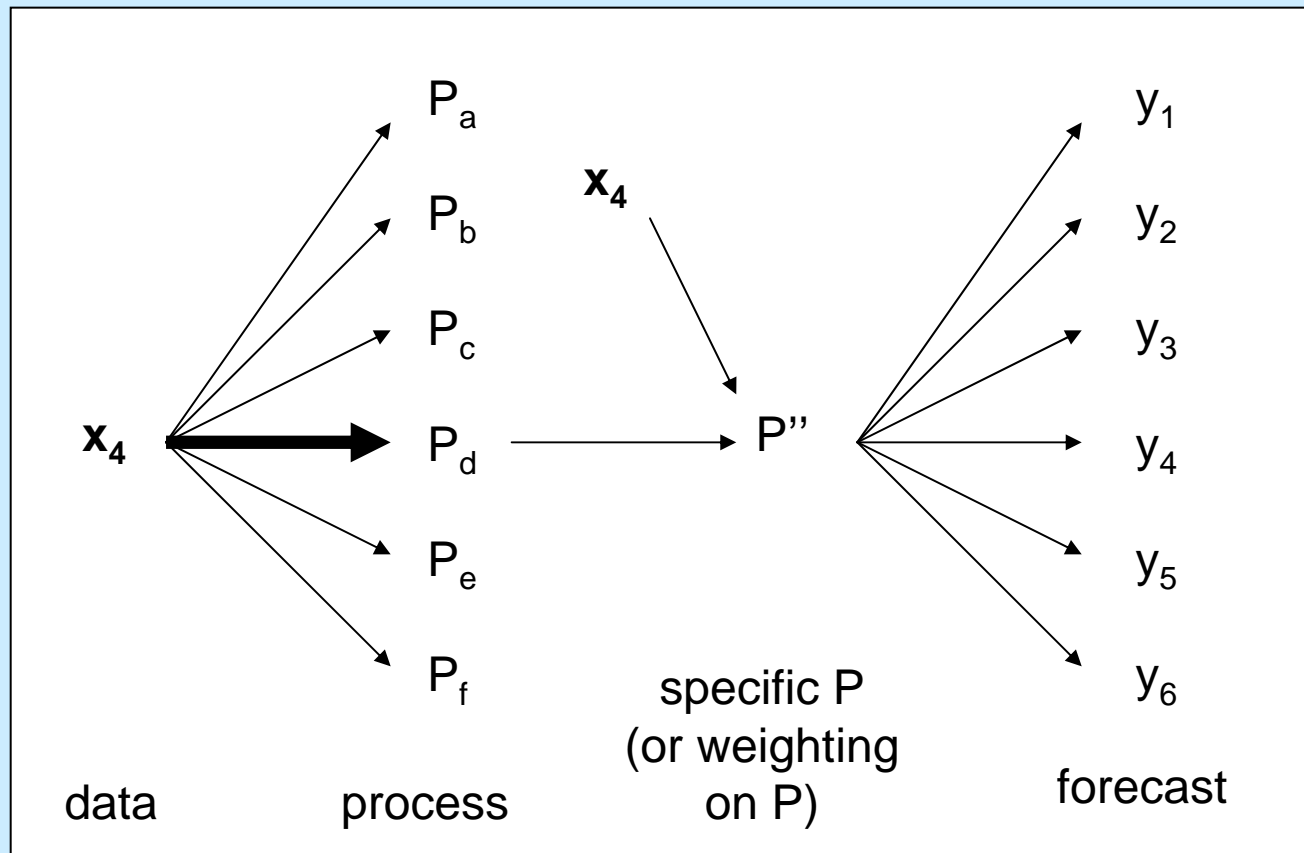
National Marine Fisheries Service



Goal: provide a well-behaved estimate of quasi-extinction probabilities given time series data from species of conservation concern



# Dealing with process uncertainty: A common approach is model selection

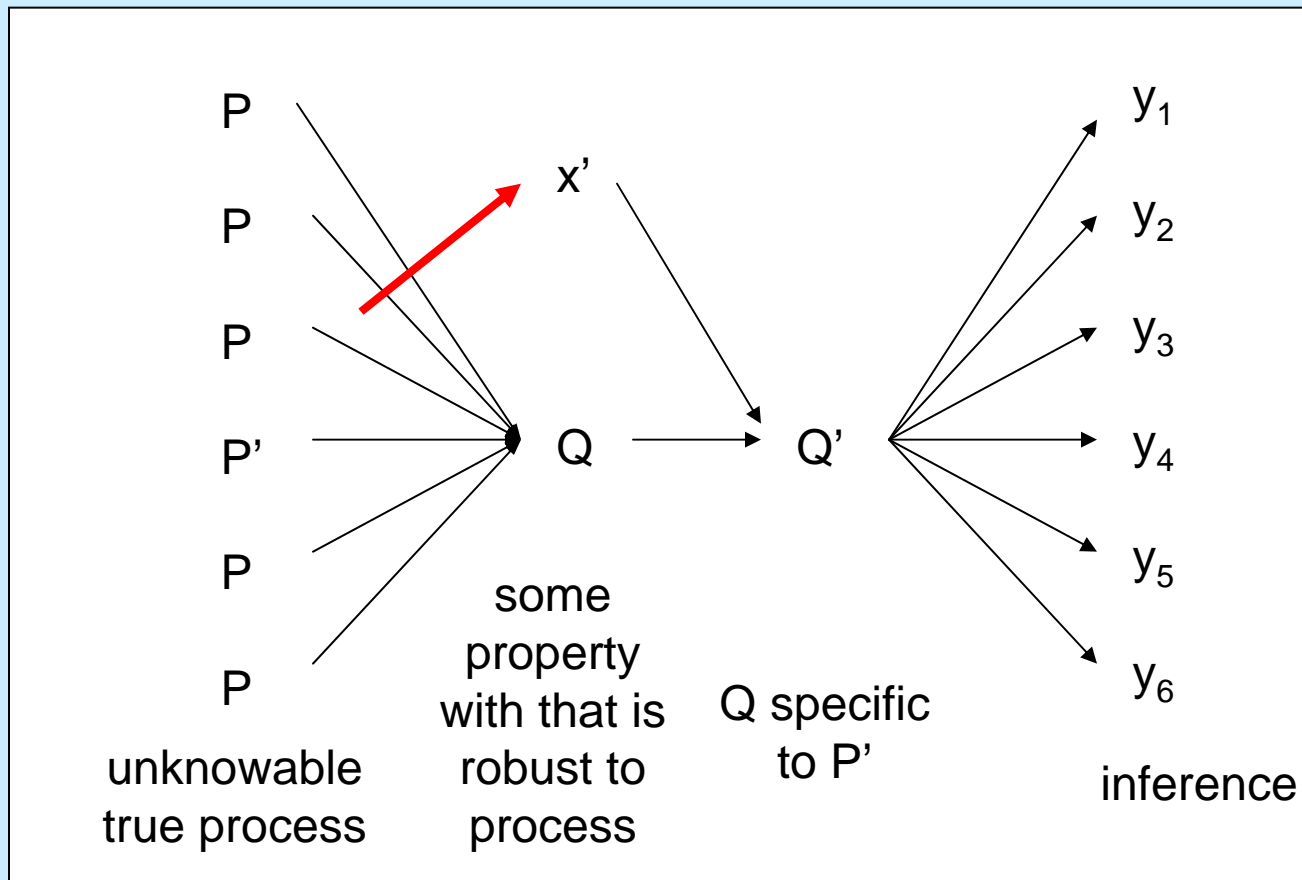


Model weighting

Parameter estimation

Extrapolation

# Dealing with model uncertainty: An approach from mathematical statistics

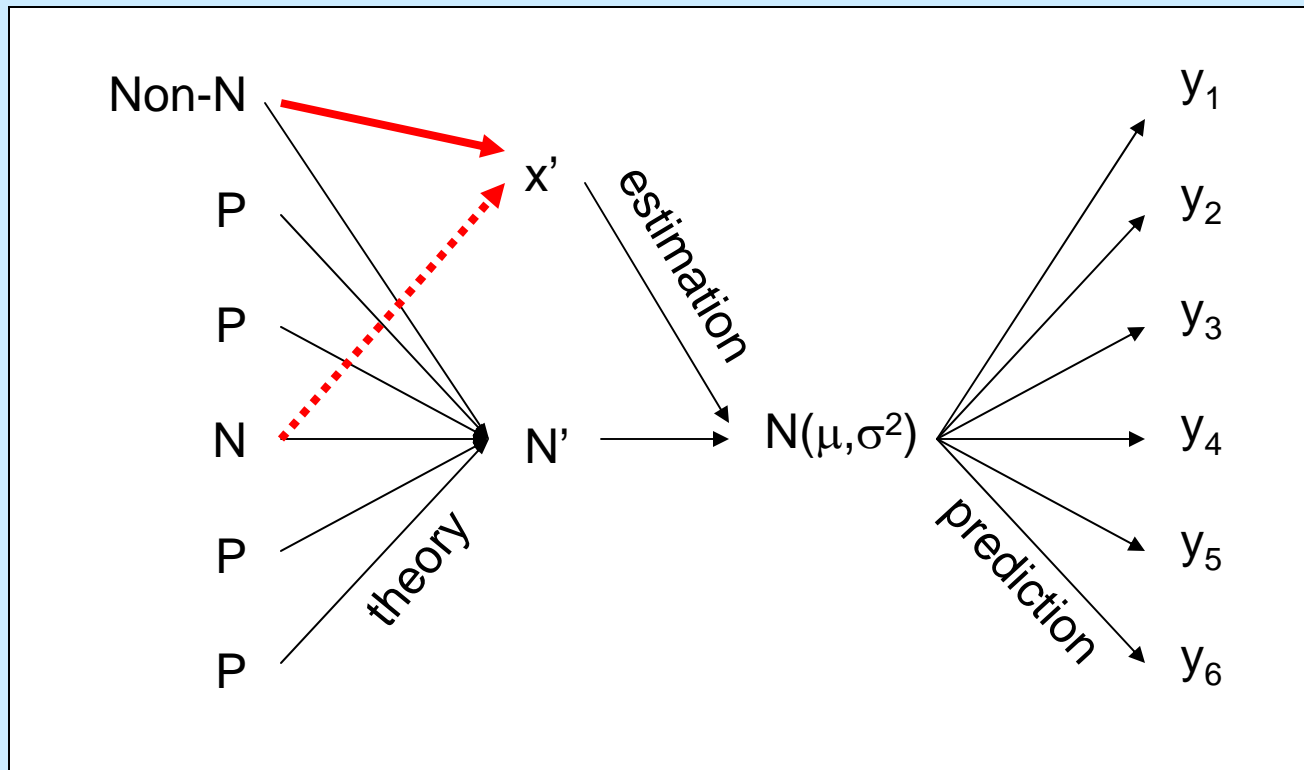


# An analogy from statistics: what's the distribution of the mean of a large sample?

Data = measurements  $x_1, x_2, \dots, x_n$  from some unknown  
distribution

Want to make inference about  $\frac{1}{n} \sum_{i=1}^n x_i$

Central Limit Theorem says that under broad conditions  
(whatever distribution  $x$ 's are from and not too non-i.i.d), mean  
→ Gaussian distribution with some mean and variance.

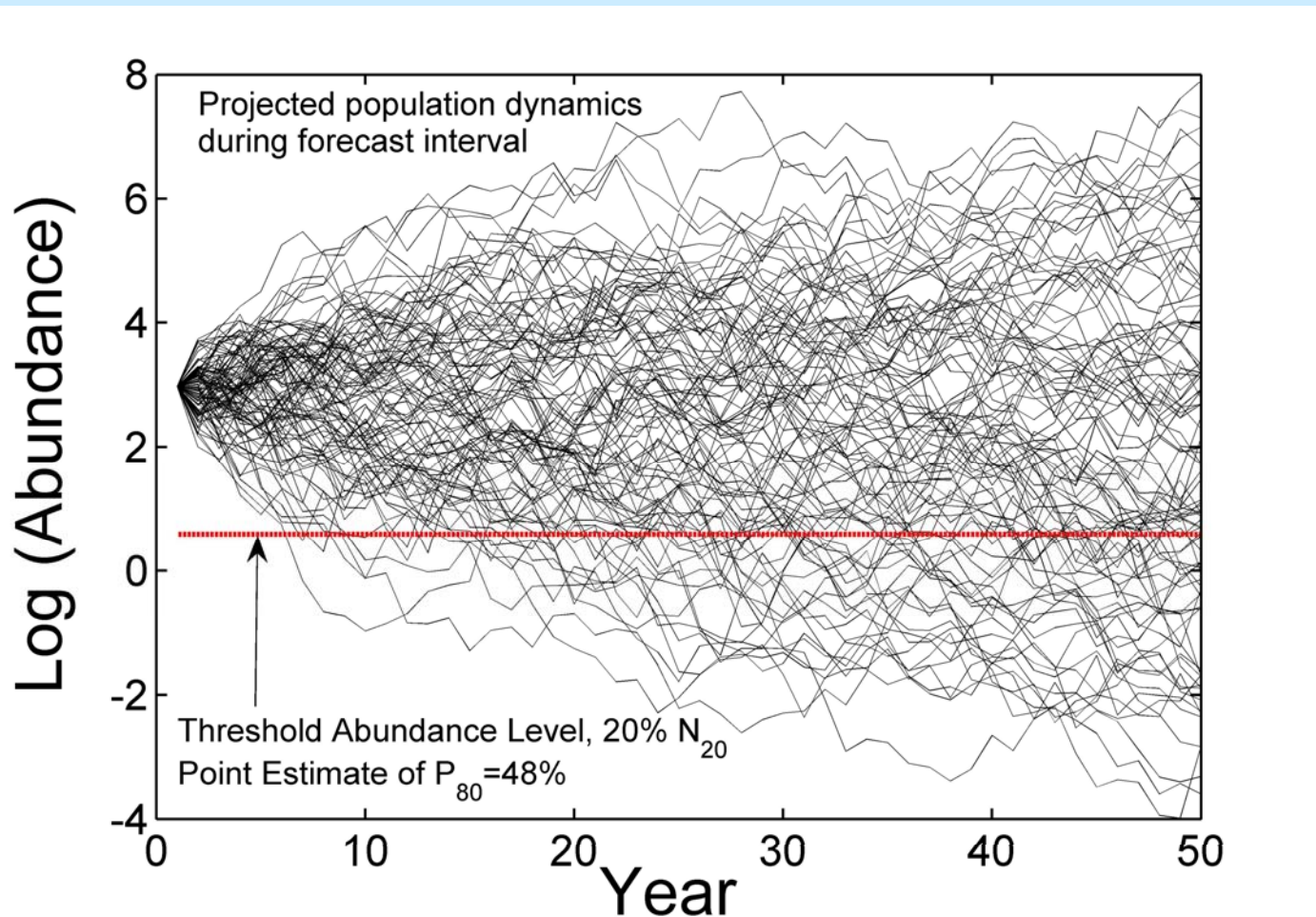


Unknown  
true  
process

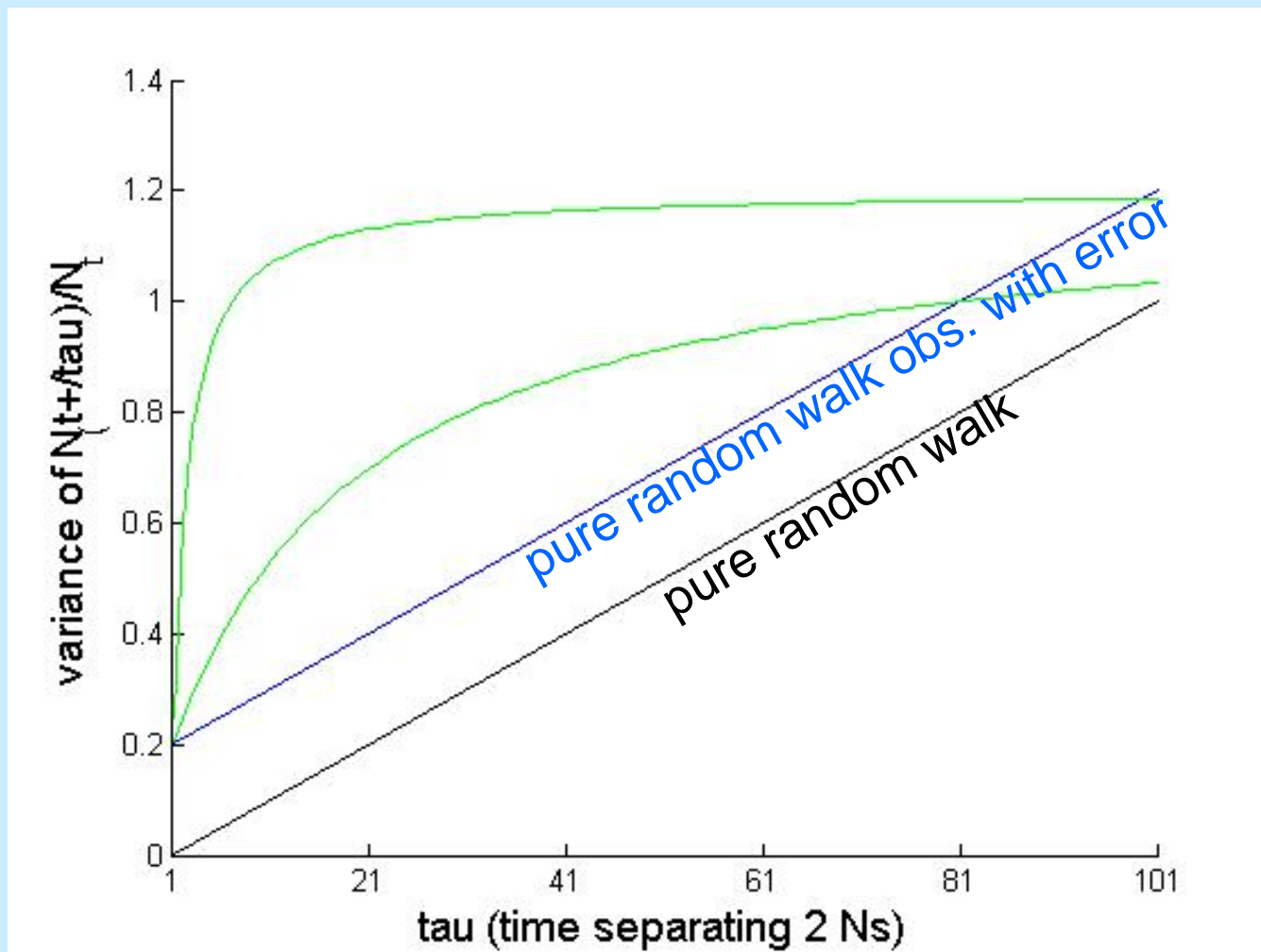
Large  
sample  
mean  
(CLT)

Estimation of large  
sample mean from  
small sample

Why expect the existence of a simple stochastic process to approximate quasi-extinction probabilities?



# Common patterns of relating how variance increases in stochastic population time series





# Corrupted random walk

Pure discrete random walk (RW)

+ corruption (CRW)

$$\log(N_t) = \log(N_{t-1}) + \mu + \eta_{t-1}$$

Normal

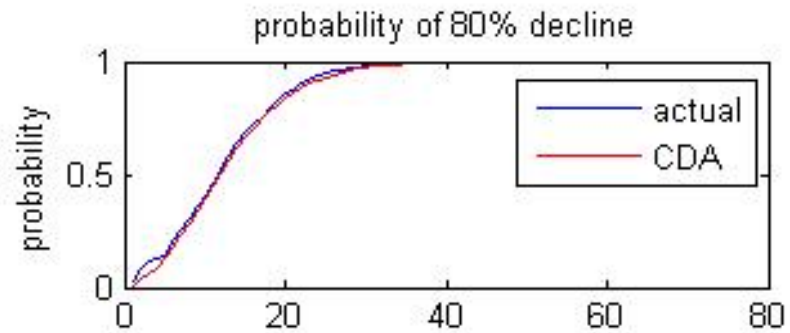
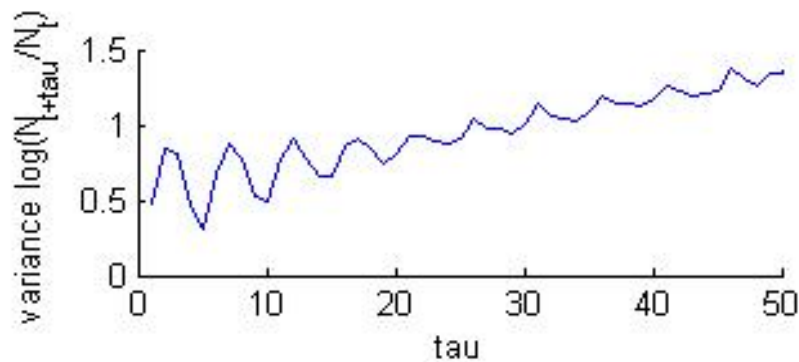
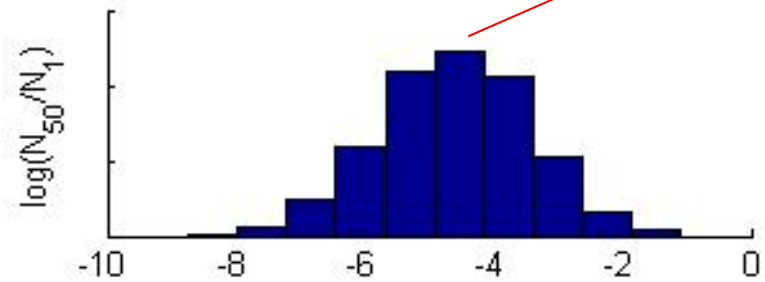
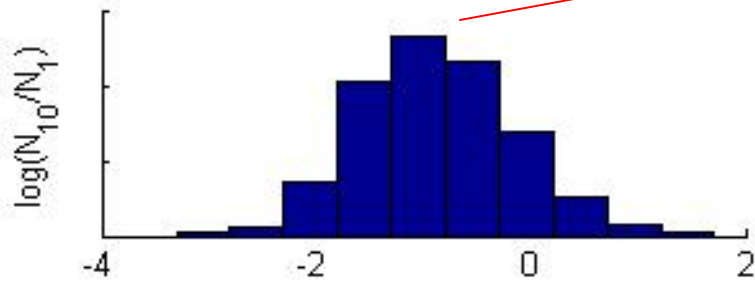
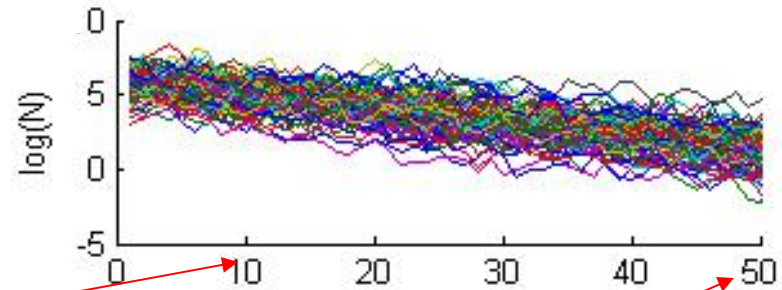
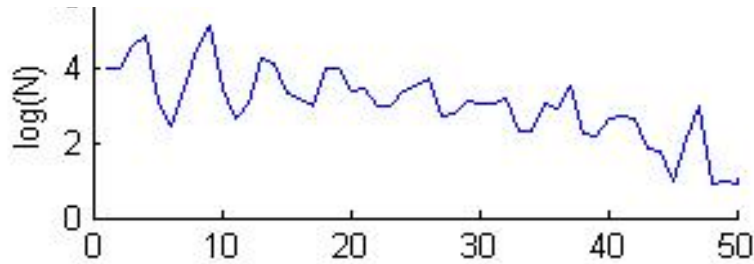
$$\mathbf{y}_t = \log(N_t) + \varepsilon_t$$

Exponential growth with viability in year to year growth rates

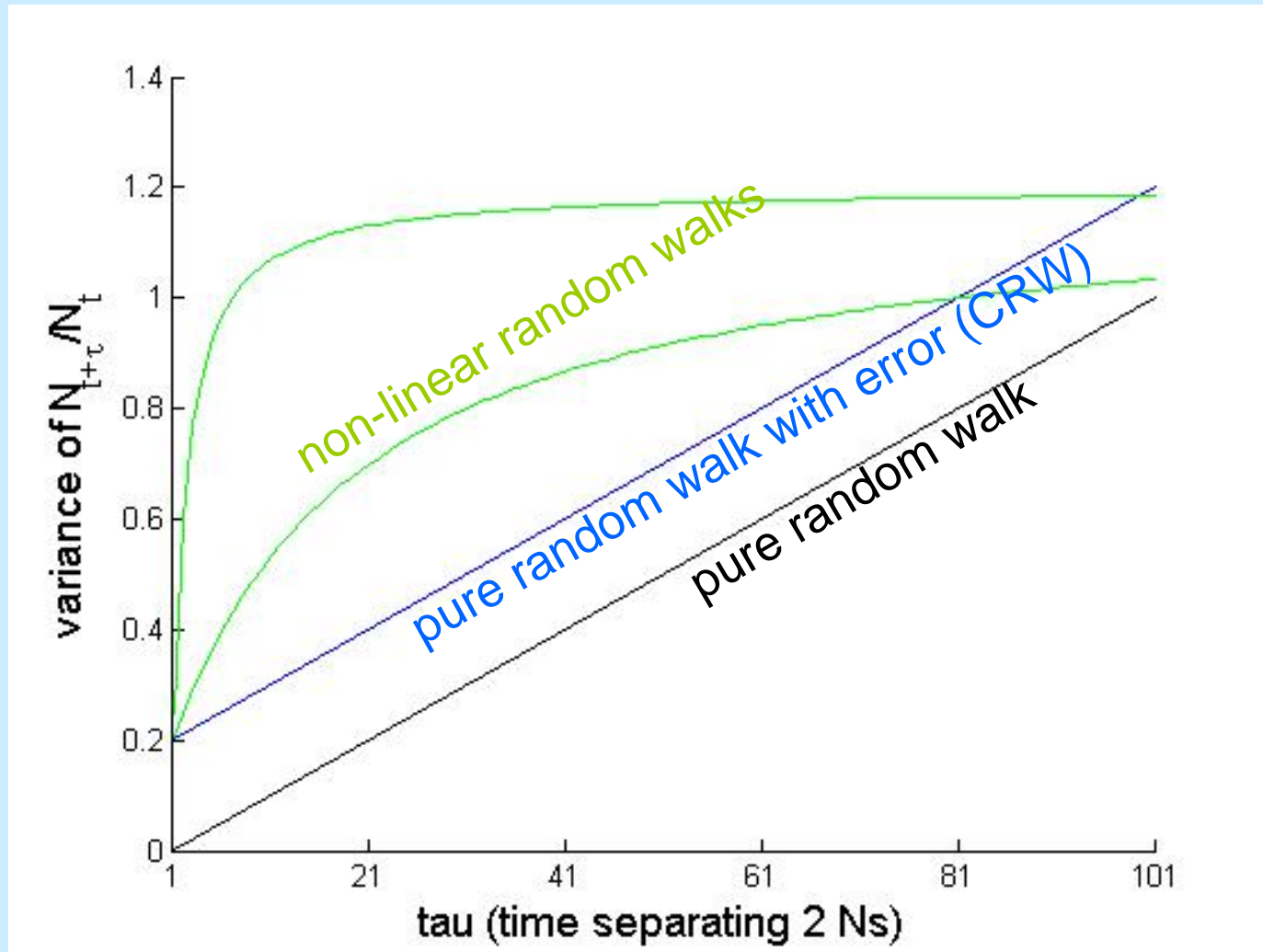
Variability that doesn't feed back into the process (e.g. measurement error, cycles)

# Stochastic age-structured models are an example where a CRW approximation works

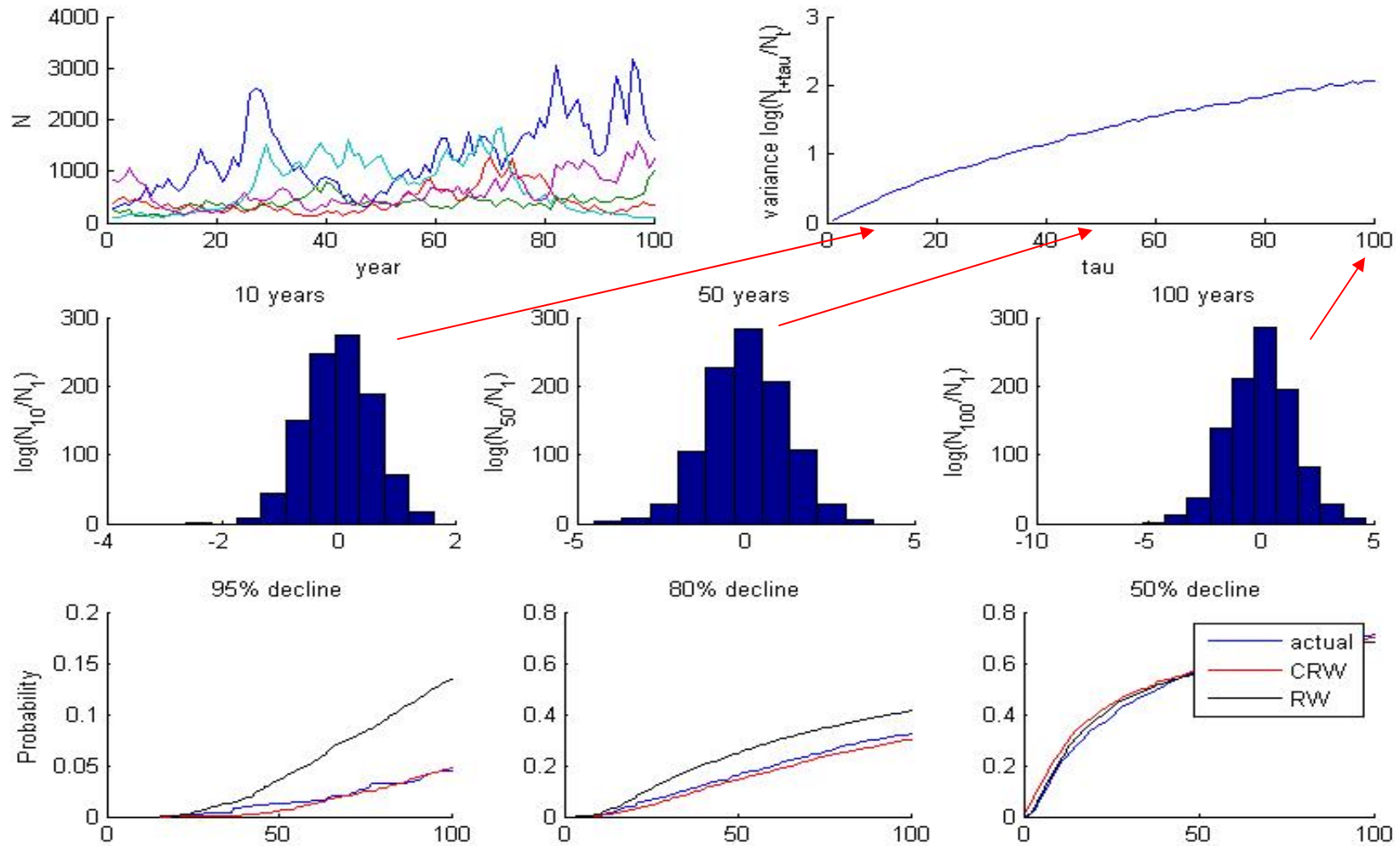
Age-structured stochastic Leslie matrix model for chinook salmon



# What about density-dependent processes?



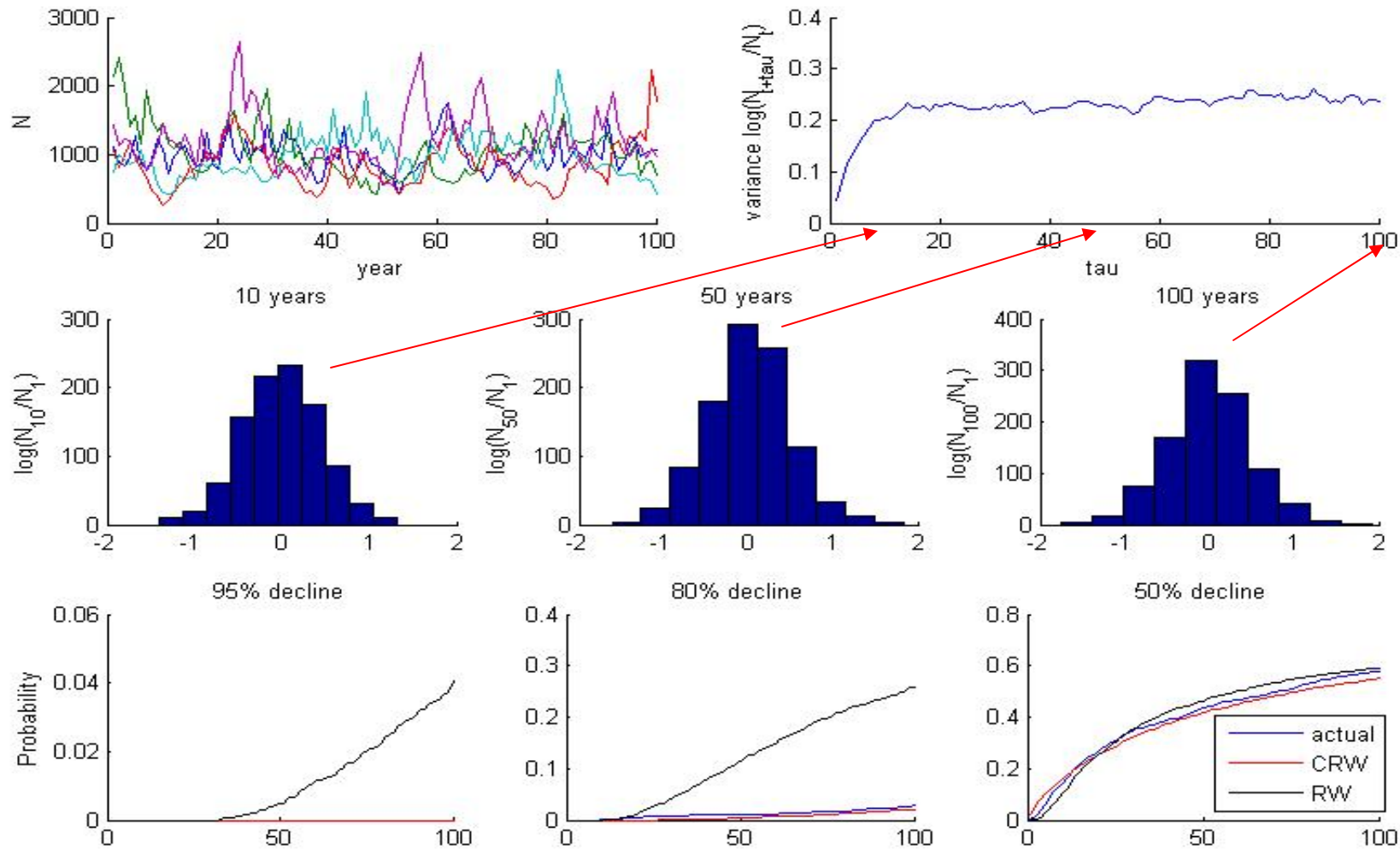
# Low density-dependent population processes can still be approximated by a CRW



Stochastic ricker

time horizon

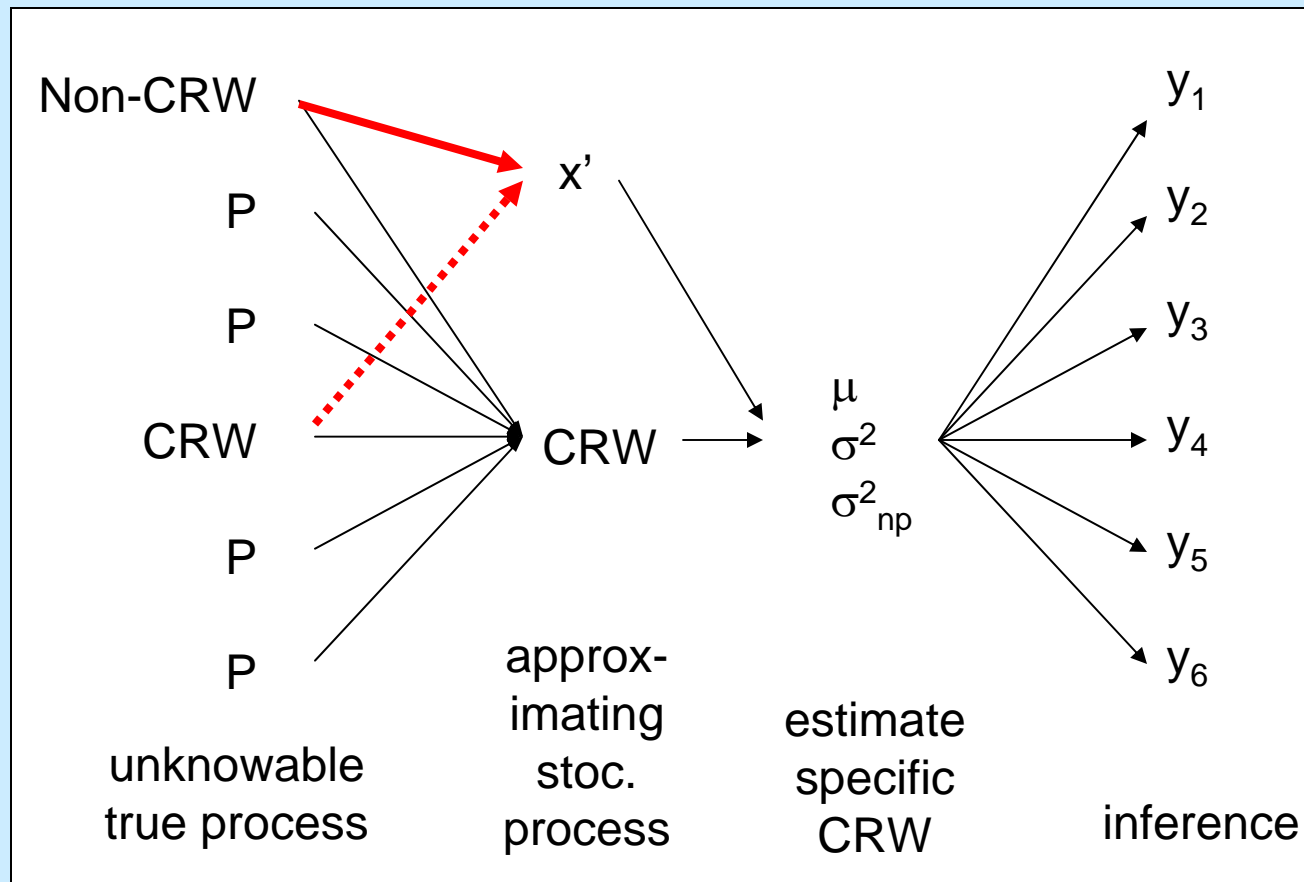
# More obviously density-dependent processes may also be approximated



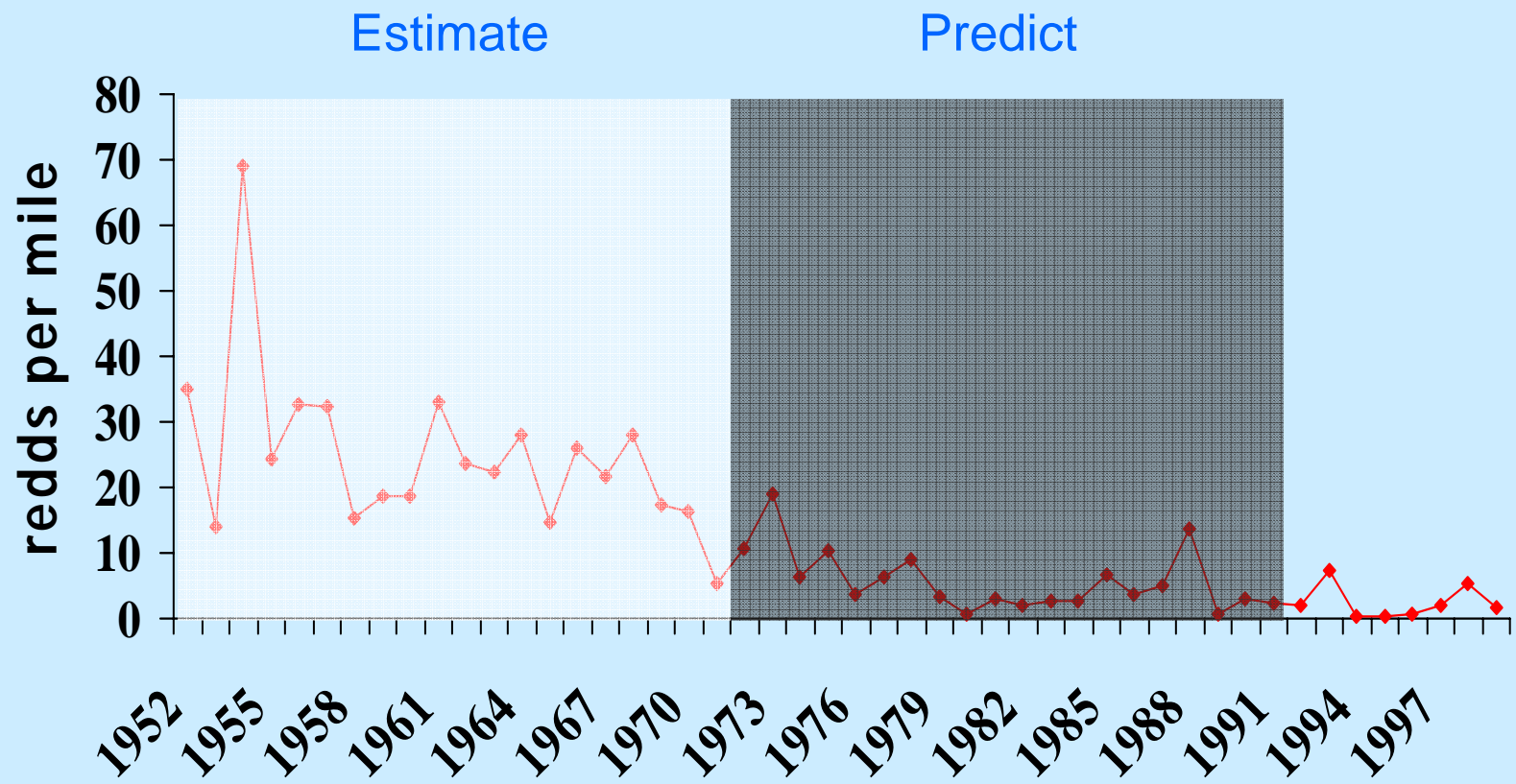
Stochastic ricker

time horizon

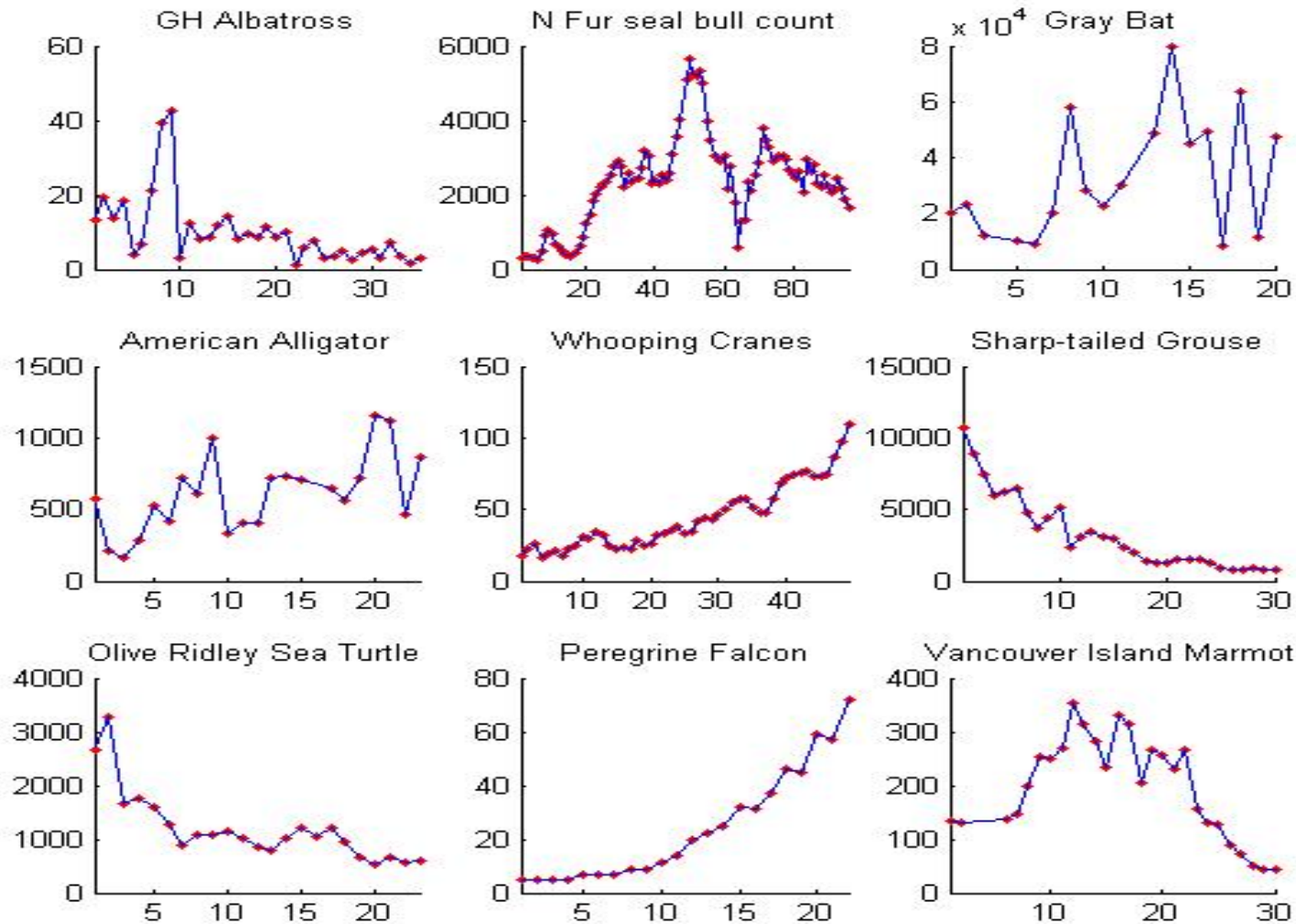
# Existence of an approximating stochastic process is one thing, estimation it is another



# Using cross-validations with real time series to study CRW approximations for quasi-extinction prediction



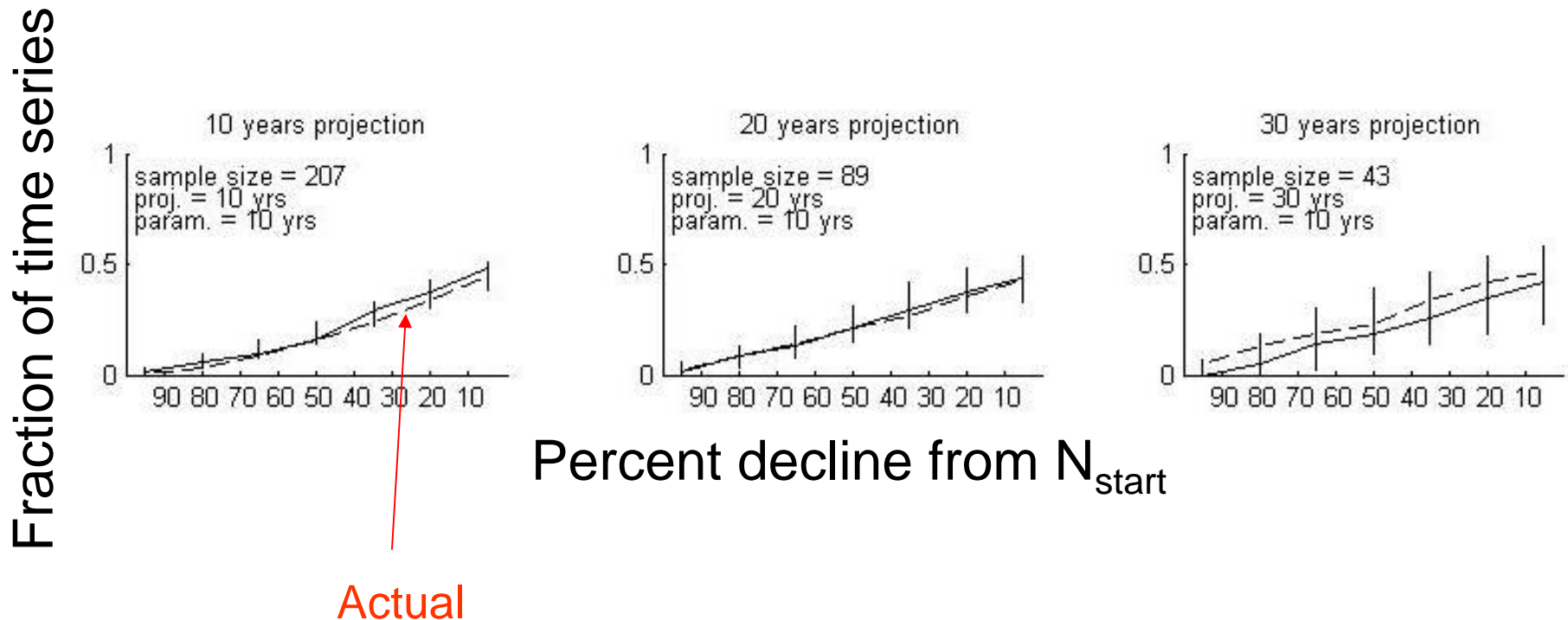
# Database of species of conservation concern: 117 time series 20-50 yrs long mammal and bird dominated



Holmes, Fagan et al. (2006)



# Low Bias: close correspondence between the expected and observed fraction of quasi-extinctions in the dataset as a whole

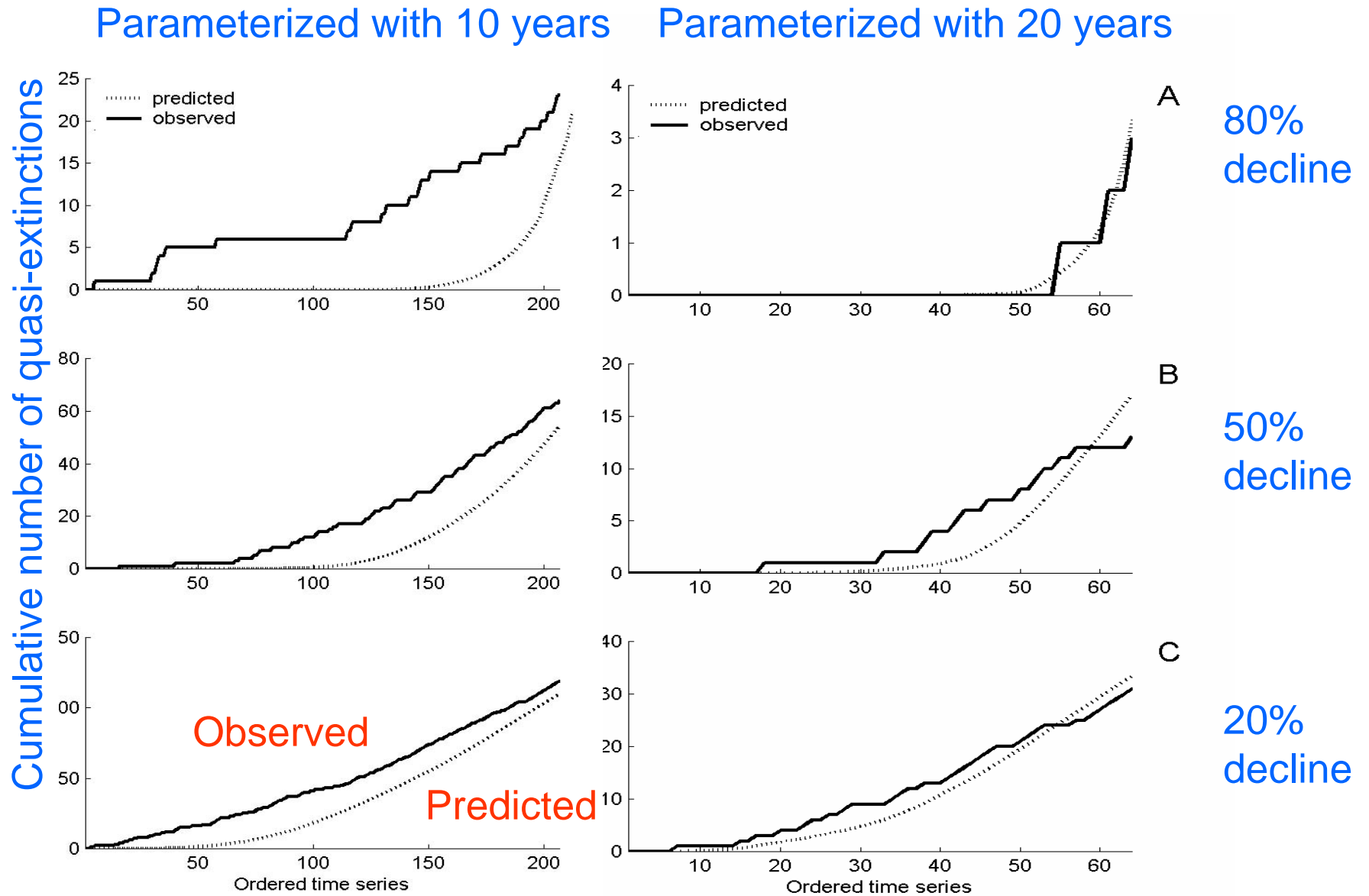


All examples use 10 years to parameterize and a kalman filter estimation

To look at correspondence, I examined cumulative quasi-extinctions

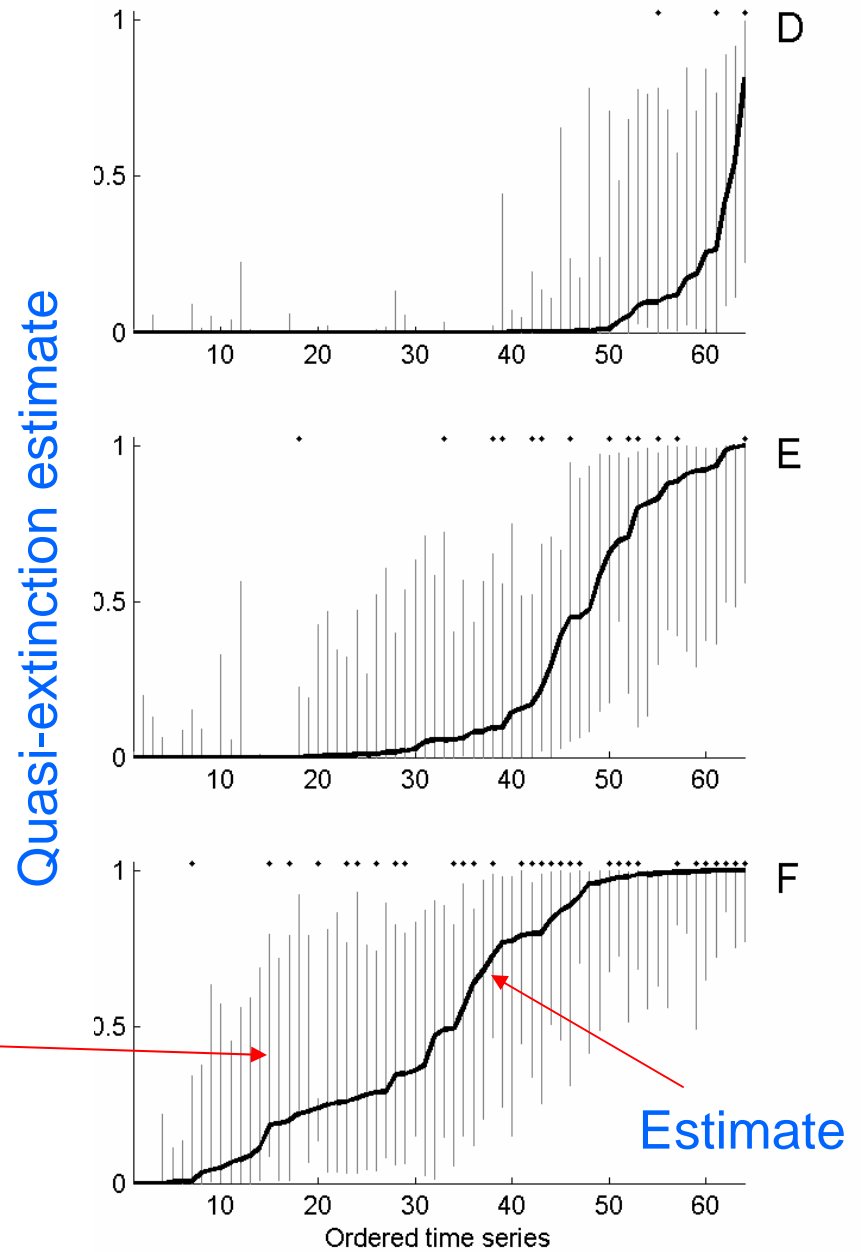
| Estimate | Expected Cumulative | Quasi-extinctions | Actual Cumulative |
|----------|---------------------|-------------------|-------------------|
| 0        | 0                   | 0                 | 0                 |
| .1       | .1                  | 0                 | 0                 |
| .12      | .22                 | 1                 | 1                 |
| .12      | .34                 | 0                 | 1                 |
| .15      | .49                 | 1                 | 2                 |
| .3       | .79                 | 0                 | 2                 |
| .35      | 1.14                | 0                 | 2                 |
| .7       | 1.84                | 1                 | 3                 |
| 1        | 2.84                | 1                 | 4                 |

# Discrimination depends on parameterization



CRW projecting 10 years; kalman filter

Wide confidence intervals quasi-extinctions but not 0 to 1 when I use at least 20 years of data.



Kalman filter; 20 years parameterization

# Conclusions

- Theoretical reasons to think that parsimonious approximations for first-passage probabilities exist
- Cross-validations with datasets (SOC, Salmon) suggest that a reasonable CRW can be estimated for 20-30 yr projections
- So far, properties of the estimates are well-characterized even when CIs are wide.

## Some important results I didn't show

- Talk focused on CRW, but the analysis actually compares CRW and RW approximations.
- This dataset is not overly plagued by non-process error *and RW approx. also works well.*
- But CRW worked consistently better in our other cross-validations using large salmon data (Holmes and Fagan 2002), in predator-prey (Sabo & Gerber 2006) and density-dependent simulations (Holmes, Sabo & Viscido, in prep).
- We have separated out those time series representing extinction events (Fagan and Holmes 2006)

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